

Weak processes in light nuclei

Saori Pastore
Topical Collaboration Meeting
Santa Fe NM - May 2020



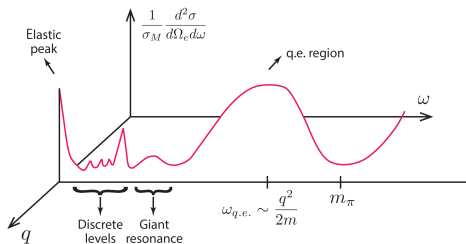
Lorenzo Andreoli (PD) Garrett King (GS) Sam Brusilow (UG)

Collaborators:

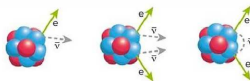
Piarulli (WashU) Carlson & Gandolfi (LANL) Schiavilla (ODU+JLab) Wiringa (ANL)
Baroni (USC) Girlanda (Salento U.) Marcucci & Viviani (Pisa U/INFN)
Mereghetti & Dekens & Cirigliano & Graesser (LANL)
de Vries (UMass-Amherst) van Kolck (AU+CNRS/IN2P3)

Resources: DOE-ALCC 0.39 MNH for "Low Energy Neutrino-Nucleus Interactions", SP *et al.* 2019

Towards a coherent and unified picture of lepton-nucleus interactions



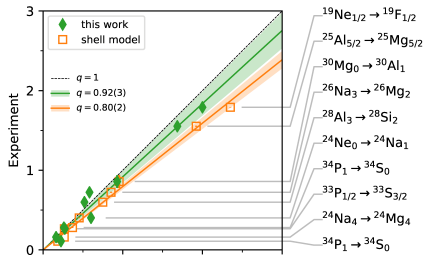
- * $\omega \sim \text{few MeV}, q \sim 0$: EM-decay, β -decay, $\beta\beta$ -decay
- * $\omega \sim \text{few MeV}, q \sim 10^2 \text{ MeV}$: μ -capture, Neutrinoless $\beta\beta$ -decay
- * $\omega \lesssim \text{tens MeV}$: Nuclear Rates for Astrophysics
- * $\omega \sim 10^2 \text{ MeV}$: Accelerator neutrinos, e^- and ν -nucleus scattering



Standard β Decay Double β Decay Neutrinoless Double β Decay

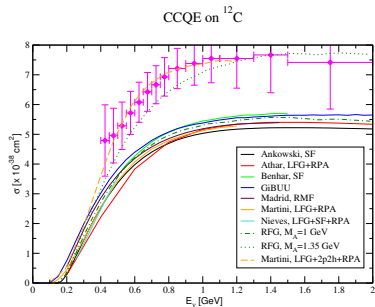
Neutrinos and Nuclei: Challenges and Opportunities

Beta Decay Rate



Gysbers *et al.* [Nature Phys.15\(2019\)](#)

Neutrino-Nucleus Scattering



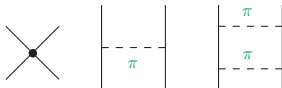
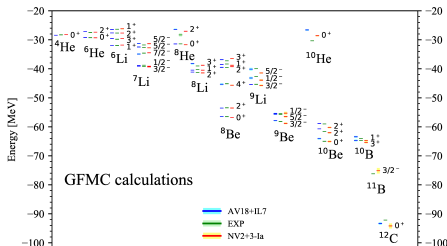
Alvarez-Ruso [arXiv:1012.3871](#)

Nuclear Interactions

The nucleus is made of A non-relativistic interacting nucleons and its energy is

$$H = T + V = \sum_{i=1}^A t_i + \sum_{i<j} v_{ij} + \sum_{i<j<k} V_{ijk} + \dots$$

where v_{ij} and V_{ijk} are **two-** and **three-**nucleon operators based on EXPT data fitting and fitted parameters subsume underlying QCD

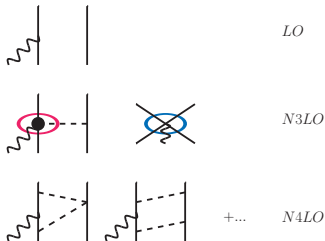


- * QMC: AV18+UIX / AV18+IL7
Wiringa+Schiavilla+Pieper et al.
- * QMC: NN(N3LO)+3N(N2LO) (π &N& Δ)
Piarulli et al. - Norfolk Potential NV2+3

Nuclear Interactions and Axial Currents

$$H = T + V = \sum_{i=1}^A t_i + \sum_{i<j} v_{ij} + \sum_{i<j<k} V_{ijk} + \dots$$

so far results are available with AV18+IL7 ($A \leq 10$)
and SNPA or chiral currents (*a.k.a.* hybrid calculations)



A. Baroni *et al.* PRC93(2016)015501

H. Krebs *et al.* Ann.Phys.378(2017)

* c_3 and c_4 are taken from Entem and Machleidt PRC68(2003)041001 & Phys.Rep.503(2011)1

* c_D fitted to GT m.e. of tritium
Baroni *et al.* PRC94(2016)024003

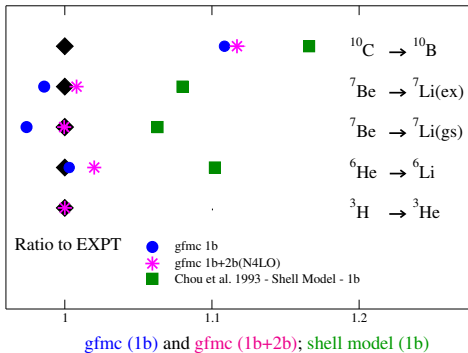
* cutoffs $\Lambda = 500$ and 600 MeV

* include also N4LO 3b currents (tiny)

* derived by Park *et al.* in the '90
used at tree-level in many calculations (Song-Ho, Kubodera, Gazit, Marcucci, Lazauskas, Navratil ...)

* pion-pole at tree-level derived
by Klos, Hoferichter *et al.* PLB(2015)B746

Single Beta Decay Matrix Elements in $A = 6-10$



SP *et al.* PRC97(2018)022501

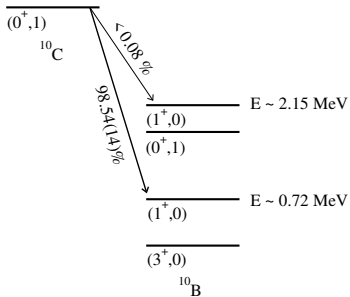
A. Baroni *et al.* PRC93(2016)015501 & PRC94(2016)024003

Based on $g_A \sim 1.27$ no quenching factor

GT in ^3H is fitted to expt - 2b give a 2% additive contribution to 1b prediction

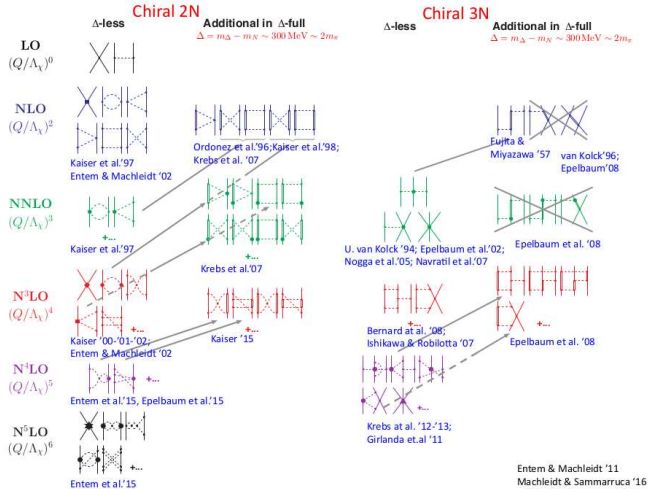
* similar results were obtained with MEC currents

* data from TUNL, Suzuki *et al.* PRC67(2003)044302, Chou *et al.* PRC47(1993)163

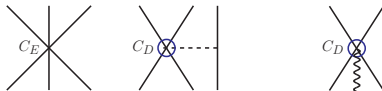
^{10}B 

- * In ^{10}B , ΔE with same quantum numbers $\sim 1.5 \text{ MeV}$
- * In $A = 7$, ΔE with same quantum numbers $\gtrsim 10 \text{ MeV}$

Chiral calculations of beta decay m.e.'s: Nuclear Interaction

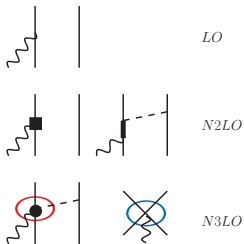


Nuclear Interactions and Axial Currents



we use

Norfolk chiral 2- and 3-body interactions by [Piarulli *et al.*](#) and consistent axial currents up to N3LO (tree-level) by [A. Baroni *et al.*](#)



* c_3 and c_4 are taken from Krebs *et al.* [Eur.Phys.J.\(2007\)A32](#)

* (c_D, c_E) fitted to:

1. trinucleon B.E. and *nd* doublet scattering length **NV2+3 models**

or

2. trinucleon B.E. and GT m.e. of tritium **NV2+3* models**

Fitting Strategies for (c_D, c_E)

Local chiral 3N potential with Δ 's

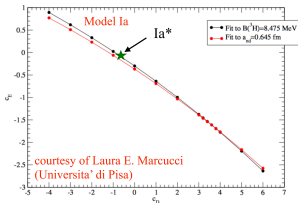
Inclusion of 3N forces at N2LO:



1) Fit to:

- ▶ $E_0(^3\text{H}) = -8.482$ MeV
- ▶ $^2a_{nd} = (0.645 \pm 0.010)$ fm

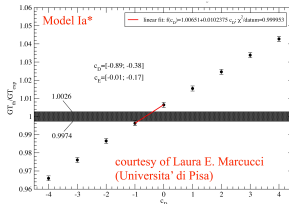
Model	c_D	c_E
Ia	3.666	-1.638
Ib	-2.061	-0.982
IIa	1.278	-1.029
IIb	-4.480	-0.412



2) Fit to:

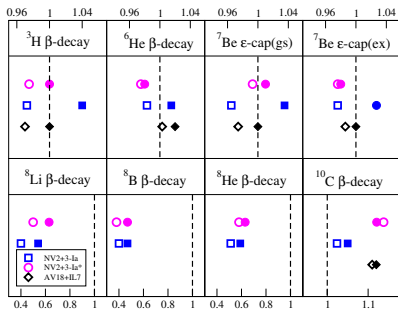
- ▶ $E_0(^3\text{H}) = -8.482$ MeV
- ▶ GT m.e. in ^3H β -decay

Model	c_D	c_E
Ia*	-0.635(255)	-0.09(8)
Ib*	-4.705(285)	0.550(150)
IIa*	-0.610(280)	-0.350(100)
IIb*	-5.250(310)	0.05(180)



Courtesy of M. Piarulli and the Pisa-group

Single Beta Decay Matrix Elements in $A = 6-10$



NV2+3-Ia and NV2+3-Ia*; AV18+IL7 from SP *et al.* PRC97(2018)022501

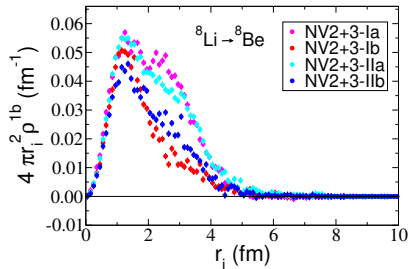
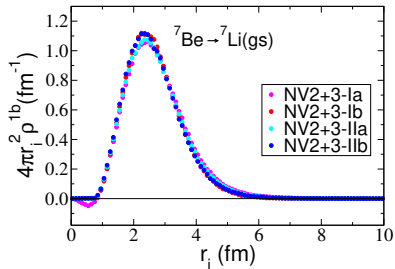
1b (empty symbols) and 2b (full symbols) GFMC predictions

King *et al.* arXiv:2004.05263

* similar results were obtained with MEC currents

* data from TUNL, Suzuki *et al.* PRC67(2003)044302, Chou *et al.* PRC47(1993)163

Single Beta Decay Matrix Element Densities in chiEFT



King *et al.* arXiv:2004.05263

Some Numbers

	NV2+3-Ia	NV2+3-Ia*
c_D	3.666	-0.635
c_E	-1.638	-0.090
z_0	0.090	1.035

Contact current

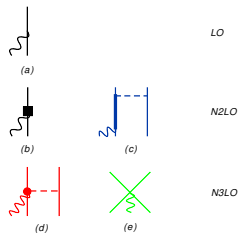
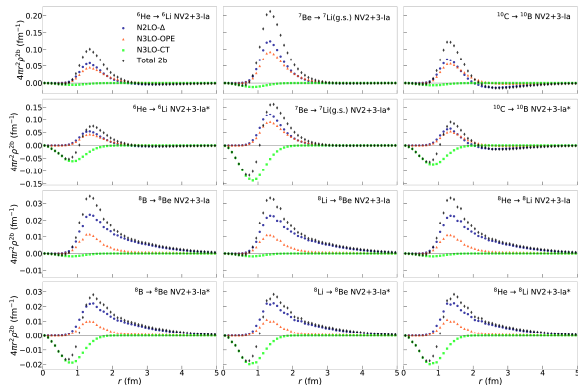
$$\mathbf{j}_{5,a}^{\text{N}^3\text{LO}}(\mathbf{q}; \text{CT}) = z_0 e^{i\mathbf{q}\cdot\mathbf{R}_{ij}} \frac{e^{-\tilde{r}_{ij}^2}}{\pi^{3/2}} (\boldsymbol{\tau}_i \times \boldsymbol{\tau}_j)_a (\boldsymbol{\sigma}_i \times \boldsymbol{\sigma}_j),$$

and LECs

$$z_0 = \frac{g_A}{2} \frac{m_\pi^2}{f_\pi^2} \frac{1}{(m_\pi R_S)^3} \left[-\frac{m_\pi}{4g_A \Lambda_\chi} c_D + \frac{m_\pi}{3} (c_3 + 2c_4) + \frac{m_\pi}{6m} \right],$$

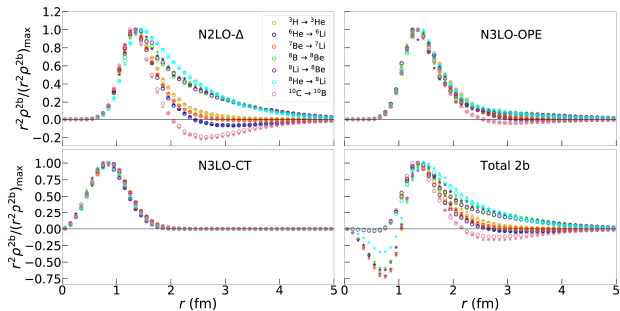


Two-body transition densities: $A = 3 - 10$



King et al. arXiv:2004.05263

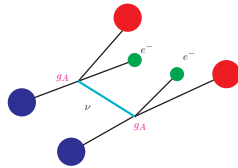
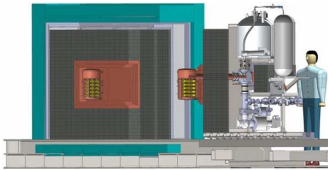
Two-body transition densities: Scaling



NV2+3-Ia empty circles – NV2+3-Ia* stars
different colors refer to different transitions

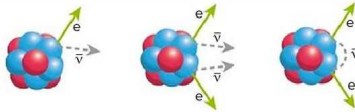
King *et al.* arXiv:2004.05263

Neutrinoless Double Beta Decay



“The average momentum is about **100 MeV**, a scale set by the average distance between the two decaying neutrons” *cit. Engel&Menéndez*

* Decay rate \propto (nuclear matrix elements)² \times $\langle m_{\beta\beta} \rangle^2$ *

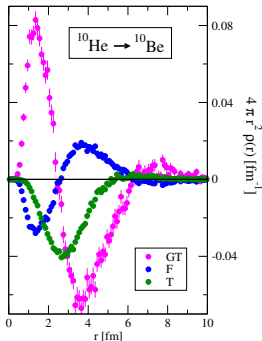
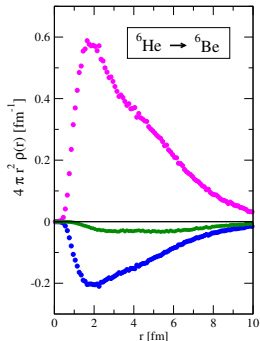


Standard β Decay

Double β Decay

Neutrinoless Double β Decay

F, GT, and T Transition Densities



* $\Delta T = 0$

${}^6\text{He}(1) \rightarrow {}^6\text{Be}(1)$

${}^8\text{He}(2) \rightarrow {}^8\text{Be}^*(2)$

${}^{10}\text{Be}(1) \rightarrow {}^{10}\text{C}(1)$

* $\Delta T = 2$

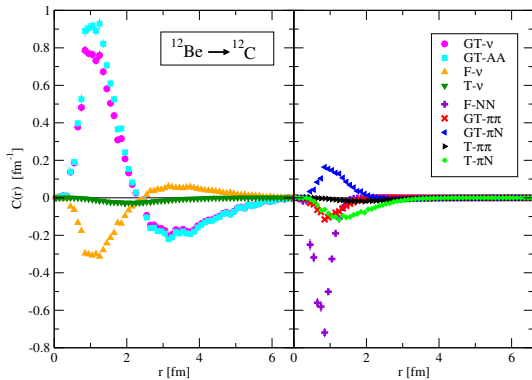
${}^8\text{He}(1) \rightarrow {}^8\text{Be}(0)$

${}^{10}\text{He}(3) \rightarrow {}^{10}\text{Be}(1)$

${}^{12}\text{Be}(2) \rightarrow {}^{12}\text{C}(0)$

$$F = \tau_{1,+} \tau_{2,+} ; \text{GT} = \tau_{1,+} \tau_{2,+} \boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2 ; \text{T} = \tau_{1,+} \tau_{2,+} S_{12}$$

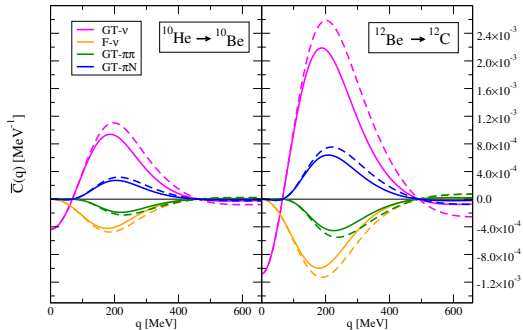
Double beta-decay Matrix Elements



SP et al. PRC97(2018)014606

Momentum Dependence and Sensitivity to N2LO effects

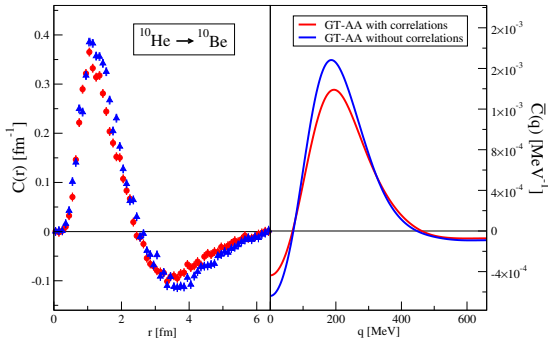
i.e., ‘dipole’ nucleonic form factors and $\nu_v^{\text{N2LO-loop}}$



- * Peaks at ~ 200 MeV
- * Form factors on/off $\rightarrow \sim 10\%$ variation same size as $\nu_v^{\text{N2LO-loop}}$ from Cirigliano *et al.* arXiv:1710.01729
- * $A = 10$ highly suppressed w.r.t. $A = 12$ (clusterization matter?)
- * $A = 12$ ‘most similar’ to experimental cases

SP *et al.* PRC97(2018)014606

Sensitivity to 'pion-exchange-like' correlations

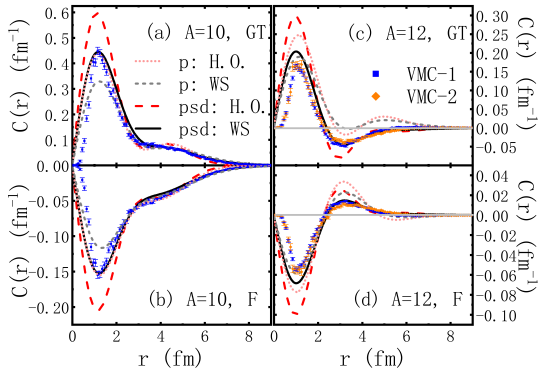


- * no 'pion-exchange-like' correlation operators U_{ij}
- * yes 'pion-exchange-like' correlation operators U_{ij}
- * $\sim 10\%$ increase in the matrix elements corresponds to a ' g_A -quenching' of ~ 0.95
- * as opposed to ~ 0.83 found in $A = 10$ single beta decay

* Correlations reduce the m.e.'s (also true for μ 's and GT's) *

Benchmark with Shell Model

Model dependence
size's space p vs psd & H.O. vs W.S. wave functions



X. Wang *et al.* Phys. Lett. B 798 (2019) 134974

Summary and Outlook

Two-nucleon correlations and two-body electroweak currents are crucial to explain available experimental data of both static (ground state properties) and dynamical (cross sections and rates) nuclear observables

- * We validate the computational framework vs electromagnetic data
 - * Two-body currents can give $\sim 30 - 40\%$ contributions and improve on theory/EXPT agreement
 - * Calculations of β^- and $\beta\beta^-$ -decay m.e.'s in $A \leq 12$ indicate two-body physics (currents and correlations) is required
 - * Short-Time-Approximation to evaluate ν -A scattering in $A > 12$ nuclei is in excellent agreement with exact calculations and data
- * We are developing a coherent picture for lepton-nucleus interactions *